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## An Efficacy Study of the Algebra II Version 10 Course

Florida Virtual School

[Report 455, December 2012]

## Contents

Executive Summary ..... 2
Research Design ..... 4
Research Questions ..... 4
Course Description ..... 4
Description of the Research Sample ..... 6
Description of the Assessments ..... 7
Data Analyses and Results ..... 9
Results for Each Module ..... 10
Module 1 ..... 11
Module 2 ..... 14
Module 3 ..... 17
Module 4 ..... 20
Module 5 ..... 23
Module 6 ..... 26
Module 7 ..... 29
Module 8 ..... 32
Module 9 ..... 35
Conclusions ..... 38

## Executive Summary

Florida Virtual School contracted with the Educational Research Institute of America to analyze the test score data for students enrolled in the Algebra II version 10 course.

Florida Virtual School (FLVS ${ }^{\circ}$ ) is an established leader in developing and providing virtual Kindergarten through grade 12 education solutions to students worldwide. A nationally recognized e-Learning model, FLVS, founded in 1997, was the country's first state-wide Internet-based public high school. In 2000, the Florida Legislature established FLVS as an independent educational entity with a gubernatorial appointed board. FLVS is the only public school with funding tied directly to student performance.

Each course has a real-time teacher who guides each student through the coursework, which is broken down into modules. As a student works through the modules of a course, he or she will connect with the teacher to take exams online and receive discussion-based assessments over the phone. Students do the work at their own pace and on their own time, but they interact with their teachers in multiple ways--including Live Lessons, phone calls, chat, texting, and email--throughout the course.

The Algebra II course is designed to meet the Florida Next Generation Sunshine State Standards and is mapped to national standards.

Pretest/posttest comparisons of students' performance were based on nine module tests which covered the total content for the course (an extra module designated only for honors students was not included in the analysis). The results showed statistically significant gains from pretesting to posttesting for each of the nine modules. The effect size, a measure of how much gain was made, was very large in each module.

Inferential statistics were not possible for the subgroups since each group of students took a small number of randomly selected items which were not always equal in difficulty. The following differences for average scores across all 9 modules showed the following:

## Basic and Honors Students

The average pretest score for the basic students was $43 \%$ correct, and their average posttest score was $78 \%$, resulting in a gain of $35 \%$.

- The average pretest score for the honors students was 50\% correct, and their average posttest score was $87 \%$ correct, resulting in a gain of $37 \%$.


## Male and Female Students

- The average pretest score for the male students was $46 \%$ correct, and their average posttest scores was $83 \%$ correct, resulting in a gain $37 \%$.
- The average pretest score for the female students was $46 \%$ correct, and their average posttest score was $81 \%$ correct, resulting in a gain of $35 \%$.


## Lower Socio-Economic Status and Higher Socio-Economic Status Students

- The average pretest score for the lower socio-economic students was $46 \%$ correct, and their average posttest scores was $80 \%$ correct, resulting in a gain of $34 \%$.
- The average pretest score for the higher socio-economic students was $46 \%$ correct, and their average posttest score was $83 \%$, resulting in a gain of $37 \%$.


## White, Minority, and Multi-Ethnic Students

- The average pretest score for the white students was $45 \%$ correct, and their average posttest scores was $82 \%$ correct, resulting in a gain of $37 \%$.
- The average pretest score for the minority students was 49\% correct, and their average posttest score was $81 \%$, resulting in a gain of $32 \%$.
- The average pretest score for the multi-ethnic students was $47 \%$ correct, and their average posttest score was 83\% correct, resulting in a gain 36\%.


## Research Design

Carefully constructed studies are needed to determine the efficacy of online courses as these courses continue to expand to all students and provide an important education opportunity to students who cannot or choose not to otherwise attend regular school programs. In addition, the enrichment of students' educational opportunities through online courses can help to prepare students for the demands of post-secondary education and the workplace. FLVS has developed a unique approach to online course instruction in which excellent online resources are accompanied by significant direct instruction, support, and guidance from teachers. Realworld application provides unique student preparation for college and/or courses.

The use of a modular approach to course development includes pretest and posttest assessments that help to guide instruction and provide excellent data to analyze program success. This study used the pretest and posttest module scores of large numbers of students over a several year period.

## Research Questions

The following questions guided the design of the study and the data analyses:

1. Do students enrolled in the Florida Virtual School Algebra II program increase their knowledge and skills in Algebra II?
2. Do students enrolled in basic or honors courses achieve similar gains in the Florida Virtual School Algebra II program?
3. Do students with differing demographic characteristics (gender, socio-economic status, and ethnicity) achieve similar gains when enrolled in the Florida Virtual School Algebra II program?

## Course Description

The Algebra II version 10 course is designed with a total of 10 instructional modules. These modules include instructional activities to meet a specific set of standards for each module. Starting with a review of basic algebra, students learn about polynomials, quadratic equations, radical and rational expressions, exponential and logarithmic relations, and sequences and series. This course allows students to learn while having fun. Interactive examples help guide students' journey through customized feedback and praise. Mathematical concepts are applied to everyday occurrences such as earthquakes, stadium seating, and purchasing movie tickets.

Students investigate the effects of an equation on its graph through the use of technology. Students have opportunities to collaborate and work with their peers on specific lessons. Algebra II is an advanced mathematics course using hands-on activities, applications, group interactions, and the latest technology.

## Segment I:

Module 1: Review of Algebra
Module 2: Systems of Equations and Inequalities
Module 3: Factoring
Module 4: Radical Expressions
Module 5: Solving Quadratic Equations

## Segment II:

Module 6: Polynomial Functions
Module 7: Rational Expressions
Module 8: Exponents and Logarithms
Module 9: Sequences and Series
Module 10: Conic Sections (Honors only and not included in this analysis)

Besides engaging students in challenging curriculum, FLVS guides students to reflect on their learning and to evaluate their progress through a variety of assessments. Assessments can be in the form of self-checks, collaboration activities, practice lessons, multiple-choice questions, writing assignments, projects, research papers, essays, discussion-based assessments, and student discussions. State and nationally-recognized educational standards and frameworks guide assessment design. Instructors evaluate progress and provide interventions through the variety of assessments built into the course, as well as through contact with the student in other venues.

## Description of the Research Sample

The study included students enrolled in the Algebra II course between July 1, 2011 and October 30, 2012.

Tables 1 to 3 provide a description of the demographic characteristics of the students included in the analysis.

Table 1: Grade Levels of Students Comprising the Research Sample

| Grade Levels |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| 8 | 9 | 10 | 11 | 12 |
| $4 \%$ | $15 \%$ | $32 \%$ | $36 \%$ | $13 \%$ |

Table 2: Gender, Course, and Free Lunch Eligibility for Free/Reduced Lunch Program of Students Comprising the Research Sample

| Gender | Course |  | Eligible for Free Reduced Lunch <br> Program |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | Females | Basic | Honors | Yes | No |
| $44 \%$ | $56 \%$ | $56 \%$ | $44 \%$ | $26 \%$ | $74 \%$ |

Table 3: Ethnicity of Students Comprising the Research Sample

| Ethnicity |  |  |
| :---: | :---: | :---: |
| White | Minority | Multi-Ethnic |
| $54 \%$ | $20 \%$ | $26 \%$ |

## Description of the Assessments

For this Algebra II study, there are 9 module pretests and 9 module posttests (called a module test within the course). Each pretest includes 19 groups of banked test items for a total of 171 groups. To limit item exposure and promote academic integrity, each student randomly receives only one test item from the bank of items in each group. For Algebra II, each pretest group consists of 4 banked test items for a total of 684 pretest items, but each student only receives a total of 171 pretest items from those banked items spread across the 9 module pretests. Each group of items covers 1 or 2 standards, and each standard is assessed multiple times. Each group of items was also designed to measure the same set of standards at the same cognitive complexity level. This random sampling provides a broad assessment since all 684 items are included in the assessment bank, but each student takes only 19 items per module pretest, and a total of 171 pretest items across the 9 module pretests throughout the course.

Each posttest includes 20 groups of banked test items for a total of 180 groups. To limit item exposure and promote academic integrity, each student randomly receives only one test item from the bank of items for each group. For Algebra II, each posttest group consists of 5 banked test items for a total of 900 posttest items, but each student only receives a total of 180 posttest items from those banked items spread across the 9 posttests. Each group of items covers 1 or 2 standards, and each standard is assessed multiple times. Each group of items was also designed to measure the same set of standards at the same cognitive complexity level. This random sampling provides a broad assessment. All 180 items are included in the assessment bank, but each student takes only 20 items per posttest and a total of 180 posttest items across the 9 module tests throughout the course.

The pretests and posttests were developed to assess the skills and strategies included in each Algebra II module. The assessments focused on the skills, strategies, and knowledge necessary for effective understanding of Algebra II knowledge and skills.

Table 4
Algebra II Module Pretests

|  | Basic and Honors |  |
| :---: | :---: | :---: |
| Pretest <br> Modules | Total \# of Banked Items | \# of Items per Student |
| Module 1 | 76 | 19 |
| Module 2 | 76 | 19 |
| Module 3 | 76 | 19 |
| Module 4 | 76 | 19 |
| Module 5 | 76 | 19 |
| Module 6 | 76 | 19 |
| Module 7 | 76 | 19 |
| Module 8 | 76 | 19 |
| Module 9 | 76 | 19 |

Table 5
Algebra II Module Posttests

|  | Basic and Honors |  |
| :---: | :---: | :---: |
| Posttest <br> Modules | Total \# of Banked Items | \# of Items per Student |
| Module 1 | 100 | 20 |
| Module 2 | 100 | 20 |
| Module 3 | 100 | 20 |
| Module 4 | 100 | 20 |
| Module 5 | 100 | 20 |
| Module 6 | 80 | 20 |
| Module 7 | 80 | 20 |
| Module 8 | 80 | 20 |
| Module 9 | 80 | 20 |

## Data Analyses and Results

Data analyses were based on the percent correct score for each student. Since different number of test items were included on the pretests and posttests, it was necessary to use percent correct scores. Only those students who were administered both a pretest and posttest for the module being analyzed are included in the data analysis.

Separate analyses were conducted for each of the modules 1 to 9 . Module 10 is for honors level students only and therefore not included in the analysis.

The following analyses were conducted to determine answers to the research questions that were the guiding focus of this study:

1. Pretest/posttest comparisons, using Paired Comparison t-tests, were used to analyze growth for each module.
2. Students were divided into two sub-groups based on their enrollment in either the basic or honors section of the Algebra II course. Pretest/posttest comparisons were then analyzed using Paired Comparison t-tests to determine if both groups increased statistically significantly.
3. Students were then divided into demographic groups based on gender, socio-economic status (determined by eligibility for free/reduced lunch program) and ethnicity (white, minority, or multi-ethnic). Pretest/posttest comparisons were then analyzed using Paired Comparison $t$-tests to determine if there were any increase differences between the various demographic groups.
4. An effect-size analysis was computed for each of the paired $t$-tests. Cohen's $d$ statistic was used to determine the effect size. This statistic provides an indication of the strength of the treatment effect regardless of the statistical significance. Cohen's $d$ statistic is interpreted as follows:
. 2 = small effect
. 5 = medium effect
.8 = large effect

## Results for Each Module

Each of the three research questions are analyzed for each module:

1. Do students enrolled in the Florida Virtual School Algebra II program increase their knowledge and skills in Algebra II?
2. Do students enrolled in basic or honors courses achieve similar gains in the Florida Virtual School Algebra II program?
3. Do students with differing demographic characteristics (gender, socio-economic status, and ethnicity) achieve similar gains when enrolled in the Florida Virtual School Algebra II program?

## Module 1

This module reviews solving equations, identifying and writing linear equations and inequalities, and graphing linear equations and inequalities. Table 6 shows that the increases from pretesting to posttesting were all statistically significant ( $\leq .0001$ ) and the effect sizes were all large. As expected, the honors students scored higher than the basic students. Other than that difference, it appears there was little difference between the various demographic groups.

Table 6: Comparison of Pretest to Posttest Percent Correct Scores Algebra II Instructional Module 1

| Group | Number of Students | Mean | Standard <br> Deviation | t-Test | Significance | Effect <br> Size |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| All Students |  |  |  |  |  |  |
| Pretest | 4839 | 53\% | . 22 | 79.902 | $\leq .0001$ | 1.37 |
| Posttest | 4839 | 80\% | . 17 |  |  |  |
| Basic Only |  |  |  |  |  |  |
| Pretest | 2768 | 49\% | . 21 | 59.583 | $\leq .0001$ | 1.41 |
| Posttest | 2768 | 76\% | . 17 |  |  |  |
| Honors Only |  |  |  |  |  |  |
| Pretest | 2071 | 59\% | . 21 | 53.349 | $\leq .0001$ | 1.39 |
| Posttest | 2071 | 85\% | . 16 |  |  |  |
| Males Only |  |  |  |  |  |  |
| Pretest | 2163 | 55\% | . 22 | 53.679 | $\leq .0001$ | 1.30 |
| Posttest | 2163 | 80\% | . 16 |  |  |  |
| Females Only |  |  |  |  |  |  |
| Pretest | 2676 | 52\% | . 21 | 59.205 | <. 0001 | 1.38 |
| Posttest | 2676 | 79\% | . 18 |  |  |  |
| Free/Reduced Lunch Only |  |  |  |  |  |  |
| Pretest | 1351 | 52\% | . 21 | 41.953 | $\leq .0001$ | 1.34 |
| Posttest | 1351 | 77\% | . 16 |  |  |  |
| No Free/Reduced Lunch Only |  |  |  |  |  |  |
| Pretest | 3488 | 54\% | . 22 | 68.025 | <. 0001 | 1.32 |
| Posttest | 3488 | 80\% | . 17 |  |  |  |
| Non-Minority Only |  |  |  |  |  |  |
| Pretest | 2475 | 53\% | . 21 | 61.283 | <. 0001 | 1.41 |
| Posttest | 2475 | 80\% | . 16 |  |  |  |
| Minority Only |  |  |  |  |  |  |
| Pretest | 1058 | 55\% | . 23 | 32.429 | <. 0001 | 1.23 |
| Posttest | 1058 | 78\% | . 16 |  |  |  |
| Multi-Ethnic |  |  |  |  |  |  |
| Pretest | 1306 | 53\% | . 21 | 41.046 | ¢. 0001 | 1.35 |
| Posttest | 1306 | 80\% | . 19 |  |  |  |

Figures 1, 2, and 3 provide a visual look at the increases. In general, the percentage increases were about $30 \%$ for each comparison group.

Figure 1: Algebra II Module 1
Pretest and Posttest Percent Correct Scores
All Students, Basic/Honors Comparison


Figure 2: Algebra II Module 1
Pretest and Posttest Percent Correct Scores
Males/Females \& Free/Reduced Lunch/No Free Reduced Lunch


Figure 3: Algebra II Module 1
Pretest and Posttest Percent Correct Scores
Non-Minority, Minority, \& Multi-Ethnic


## Module 2

This module reviews solving systems of linear equations by graphing, elimination, and substitution, real-world problems, and linear programming. Table 7 shows that the increases from pretesting to posttesting were all statistically significant ( $\leq .0001$ ) and the effect sizes were all large. As expected, the honors students scored higher than the basic students. Other than that difference, it appears there was little difference between the various demographic groups.

Table 7: Comparison of Pretest to Posttest Percent Correct Scores Algebra II Instructional Module 2

| Group | Number of Students | Mean | Standard Deviation | t-Test | Significance | Effect Size |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| All Students |  |  |  |  |  |  |
| Pretest | 3573 | 45\% | . 27 | 70.585 | $\leq .0001$ | 1.41 |
| Posttest | 3573 | 78\% | . 18 |  |  |  |
| Basic Only |  |  |  |  |  |  |
| Pretest | 1987 | 40\% | . 26 | 50.734 | $\leq .0001$ | 1.45 |
| Posttest | 1987 | 73\% | . 19 |  |  |  |
| Honors Only |  |  |  |  |  |  |
| Pretest | 1586 | 51\% | . 27 | 49.411 | $\leq .0001$ | 1.51 |
| Posttest | 1586 | 84\% | . 15 |  |  |  |
| Males Only |  |  |  |  |  |  |
| Pretest | 1599 | 45\% | . 28 | 48.525 | $\leq .0001$ | 1.49 |
| Posttest | 1599 | 80\% | . 18 |  |  |  |
| Females Only |  |  |  |  |  |  |
| Pretest | 1974 | 45\% | . 26 | 51.353 | $\leq .0001$ | 1.41 |
| Posttest | 1974 | 77\% | . 19 |  |  |  |
| Free/Reduced Lunch Only |  |  |  |  |  |  |
| Pretest | 971 | 44\% | . 26 | 36.635 | $\leq .0001$ | 1.43 |
| Posttest | 971 | 76\% | . 18 |  |  |  |
| No Free/Reduced Lunch Only |  |  |  |  |  |  |
| Pretest | 2602 | 46\% | . 27 | 60.337 | $\leq .0001$ | 1.44 |
| Posttest | 2602 | 79\% | . 18 |  |  |  |
| Non-Minority Only |  |  |  |  |  |  |
| Pretest | 1864 | 45\% | . 26 | 54.130 | $\leq .0001$ | 1.52 |
| Posttest | 1864 | 79\% | . 18 |  |  |  |
| Minority Only |  |  |  |  |  |  |
| Pretest | 759 | 47\% | 28 | 28.036 | <. 0001 | 1.21 |
| Posttest | 759 | 76\% | . 19 |  |  |  |
| Multi-Ethnic |  |  |  |  |  |  |
| Pretest | 950 | 45\% | . 27 | 36.570 | <. 0001 | 1.48 |
| Posttest | 950 | 79\% | . 18 |  |  |  |

Figures 4, 5, and 6 provide a visual look at the increases. In general, the percentage increases were about $25 \%$ to $30 \%$ for each comparison group.

Figure 4: Algebra II Module 2 Pretest and Posttest Percent Correct Scores All Students, Basic/Honors Comparison


Figure 5: Algebra II Module 2
Pretest and Posttest Percent Correct Scores
Males/Females \& Free/Reduced Lunch/No Free Reduced Lunch


Figure 6: Algebra II Module 2
Pretest and Posttest Percent Correct Scores
Non-Minority, Minority, \& Multi-Ethnic


## Module 3

This module covers factoring trinomials, factoring special cases, and contains an honors lesson on Pascal's triangle. Table 8 shows that the increases from pretesting to posttesting were all statistically significant ( $\leq .0001$ ) and the effect sizes were all large. As expected, the honors students scored higher than the basic students. Other than that difference, it appears there was little difference between the various demographic groups.

Table 8: Comparison of Pretest to Posttest Percent Correct Scores
Algebra II Instructional Module 3

| Group | Number of Students | Mean | Standard <br> Deviation | t-Test | Significance | Effect Size |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| All Students |  |  |  |  |  |  |
| Pretest | 3233 | 55\% | . 25 | 67.995 | $\leq .0001$ | 1.56 |
| Posttest | 3233 | 86\% | . 13 |  |  |  |
| Basic Only |  |  |  |  |  |  |
| Pretest | 1813 | 52\% | . 26 | 48.602 | $\leq .0001$ | 1.48 |
| Posttest | 1813 | 83\% | . 14 |  |  |  |
| Honors Only |  |  |  |  |  |  |
| Pretest | 1420 | 59\% | . 24 | 48.407 | $\leq .0001$ | 1.61 |
| Posttest | 1420 | 89\% | . 11 |  |  |  |
| Males Only |  |  |  |  |  |  |
| Pretest | 1443 | 55\% | . 26 | 45.649 | $\leq .0001$ | 1.56 |
| Posttest | 1443 | 87\% | . 13 |  |  |  |
| Females Only |  |  |  |  |  |  |
| Pretest | 1790 | 55\% | . 25 | 50.507 | $\leq .0001$ | 1.48 |
| Posttest | 1790 | 85\% | . 14 |  |  |  |
| Free/Reduced Lunch Only |  |  |  |  |  |  |
| Pretest | 895 | 56\% | . 25 | 34.307 | $\leq .0001$ | 1.46 |
| Posttest | 895 | 85\% | . 13 |  |  |  |
| No Free/Reduced Lunch Only |  |  |  |  |  |  |
| Pretest | 2338 | 55\% | . 26 | 58.796 | $\leq .0001$ | 1.51 |
| Posttest | 2338 | 86\% | . 13 |  |  |  |
| Non-Minority Only |  |  |  |  |  |  |
| Pretest | 1681 | 53\% | . 25 | 52.306 | $\leq .0001$ | 1.63 |
| Posttest | 1681 | 86\% | . 14 |  |  |  |
| Minority Only |  |  |  |  |  |  |
| Pretest | 709 | 59\% | . 26 | 27.693 | $\leq .0001$ | 1.25 |
| Posttest | 709 | 85\% | . 14 |  |  |  |
| Multi-Ethnic |  |  |  |  |  |  |
| Pretest | 843 | 56\% | . 26 | 34.427 | $\leq .0001$ | 1.53 |
| Posttest | 843 | 87\% | . 12 |  |  |  |

Figures 7, 8, and 9 provide a visual look at the increases. In general, the percentage increases were about $30 \%$ for each comparison group.

Figure 7: Algebra II Module 3
Pretest and Posttest Percent Correct Scores
All Students, Basic/Honors Comparison


Figure 8: Algebra II Module 3
Pretest and Posttest Percent Correct Scores
Males/Females \& Free/Reduced Lunch/No Free Reduced Lunch


Figure 9: Algebra II Module 3
Pretest and Posttest Percent Correct Scores
Non-Minority, Minority, \& Multi-Ethnic


## Module 4

This module covers adding, subtracting, multiplying, and dividing radicals as well as solving radical equations on the real and complex plane. Table 9 shows that the increases from pretesting to posttesting were all statistically significant ( $\leq .0001$ ) and the effect sizes were all large. As expected, honors students scored higher than basic students. Other than that, the descriptive data shows little difference between the various demographic groups.

Table 9: Comparison of Pretest to Posttest Percent Correct Scores Algebra II Instructional Module 4

| Group | Number of Students | Mean | Standard Deviation | t-Test | Significance | Effect Size |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| All Students |  |  |  |  |  |  |
| Pretest | 2724 | 43\% | . 25 | 76.731 | $\leq .0001$ | 1.74 |
| Posttest | 2724 | 81\% | . 18 |  |  |  |
| Basic Only |  |  |  |  |  |  |
| Pretest | 1485 | 39\% | . 25 | 53.573 | ¢. 0001 | 1.71 |
| Posttest | 1485 | 77\% | . 19 |  |  |  |
| Honors Only |  |  |  |  |  |  |
| Pretest | 1239 | 46\% | . 25 | 55.513 | <. 0001 | 1.94 |
| Posttest | 1239 | 86\% | . 15 |  |  |  |
| Males Only |  |  |  |  |  |  |
| Pretest | 1214 | 43\% | . 26 | 50.812 | $\leq .0001$ | 1.78 |
| Posttest | 1214 | 82\% | . 17 |  |  |  |
| Females Only |  |  |  |  |  |  |
| Pretest | 1510 | 42\% | . 24 | 57.686 | <. 0001 | 1.74 |
| Posttest | 1510 | 79\% | . 18 |  |  |  |
| Free/Reduced Lunch Only |  |  |  |  |  |  |
| Pretest | 750 | 42\% | . 25 | 40.047 | <. 0001 | 1.70 |
| Posttest | 750 | 79\% | . 18 |  |  |  |
| No Free/Reduced Lunch Only |  |  |  |  |  |  |
| Pretest | 1974 | 43\% | . 25 | 65.497 | <. 0001 | 1.79 |
| Posttest | 1974 | 81\% | . 18 |  |  |  |
| Non-Minority Only |  |  |  |  |  |  |
| Pretest | 1403 | 41\% | . 24 | 57.636 | $\leq .0001$ | 1.89 |
| Posttest | 1403 | 81\% | . 18 |  |  |  |
| Minority Only |  |  |  |  |  |  |
| Pretest | 600 | 45\% | . 26 | 32.806 | $\leq .0001$ | 1.57 |
| Posttest | 600 | 80\% | . 18 |  |  |  |
| Multi-Ethnic |  |  |  |  |  |  |
| Pretest | 721 | 43\% | . 25 | 39.157 | $\leq .0001$ | 1.74 |
| Posttest | 721 | 81\% | . 18 |  |  |  |

Figures 10, 11, and 12 provide a visual look at the increases. In general, the percentage increases were about $40 \%$ for each comparison group.

Figure 10: Algebra II Module 4
Pretest and Posttest Percent Correct Scores
All Students, Basic/Honors Comparison


Figure 11: Algebra II Module 4
Pretest and Posttest Percent Correct Scores
Males/Females \& Free/Reduced Lunch/No Free Reduced Lunch


Figure 12: Algebra II Module 4
Pretest and Posttest Percent Correct Scores
Non-Minority, Minority, \& Multi-Ethnic


## Module 5

This module covers methods for graphing and solving quadratics as well as contains honors lessons for piecewise functions and non-linear systems. Table 10 shows that the increases from pretesting to posttesting were all statistically significant ( $\leq .0001$ ) and the effect sizes were all large. The honors students scored higher than the basic students and there was little difference between the various demographic groups.

Table 5: Comparison of Pretest to Posttest Percent Correct Scores Algebra II Instructional Module 5

| Group | Number of Students | Mean | Standard Deviation | t-Test | Significance | Effect Size |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| All Students |  |  |  |  |  |  |
| Pretest | 2359 | 42\% | . 29 | 66.003 | $\leq .0001$ | 1.75 |
| Posttest | 2359 | 83\% | . 16 |  |  |  |
| Basic Only |  |  |  |  |  |  |
| Pretest | 1292 | 40\% | . 29 | 45.535 | $\leq .0001$ | 1.64 |
| Posttest | 1292 | 79\% | . 17 |  |  |  |
| Honors Only |  |  |  |  |  |  |
| Pretest | 1067 | 43\% | . 28 | 48.527 | <. 0001 | 1.99 |
| Posttest | 1067 | 87\% | . 14 |  |  |  |
| Males Only |  |  |  |  |  |  |
| Pretest | 1046 | 41\% | . 29 | 46.081 | $\leq .0001$ | 1.84 |
| Posttest | 1046 | 84\% | . 16 |  |  |  |
| Females Only |  |  |  |  |  |  |
| Pretest | 1313 | 42\% | . 28 | 47.465 | $\leq .0001$ | 1.73 |
| Posttest | 1313 | 82\% | . 17 |  |  |  |
| Free/Reduced Lunch Only |  |  |  |  |  |  |
| Pretest | 634 | 43\% | . 28 | 31.856 | $\leq .0001$ | 1.67 |
| Posttest | 634 | 81\% | . 16 |  |  |  |
| No Free/Reduced Lunch Only |  |  |  |  |  |  |
| Pretest | 1725 | 41\% | . 29 | 57.972 | $\leq .0001$ | 1.79 |
| Posttest | 1725 | 83\% | . 16 |  |  |  |
| Non-Minority Only |  |  |  |  |  |  |
| Pretest | 1229 | 40\% | . 27 | 51.729 | $\leq .0001$ | 1.94 |
| Posttest | 1229 | 83\% | . 16 |  |  |  |
| Minority Only |  |  |  |  |  |  |
| Pretest | 514 | 45\% | . 30 | 26.218 | <. 0001 | 1.44 |
| Posttest | 514 | 82\% | . 17 |  |  |  |
| Multi-Ethnic |  |  |  |  |  |  |
| Pretest | 616 | 42\% | . 29 | 33.058 | <. 0001 | 1.82 |
| Posttest | 616 | 84\% | . 15 |  |  |  |

Figures 13,14 , and 15 provide a visual look at the increases. In general, the percentage increases were about $40 \%$ for each comparison group.

Figure 13: Algebra II Module 5 Pretest and Posttest Percent Correct Scores
All Students, Basic/Honors Comparison


Figure 14: Algebra II Module 5
Pretest and Posttest Percent Correct Scores
Males/Females \& Free/Reduced Lunch/No Free Reduced Lunch


Figure 15: Algebra II Module 5
Pretest and Posttest Percent Correct Scores
Non-Minority, Minority, \& Multi-Ethnic


## Module 6

This module covers theorems for polynomials, graphing and solving polynomials, and an honors lesson for polynomial inequalities. Table 11 shows that the increases from pretesting to posttesting were all statistically significant ( $\leq .0001$ ) and the effect sizes were all large. The honors students scored higher than the basic students, and it appears there was little difference between the various demographic groups.

Table 11: Comparison of Pretest to Posttest Percent Correct Scores
Algebra II Instructional Module 6

| Group | Number of Students | Mean | Standard Deviation | t-Test | Significance | Effect Size |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| All Students |  |  |  |  |  |  |
| Pretest | 2605 | 43\% | . 25 | 80.038 | $\leq .0001$ | 1.99 |
| Posttest | 2605 | 84\% | . 15 |  |  |  |
| Basic Only |  |  |  |  |  |  |
| Pretest | 1490 | 40\% | . 24 | 16.133 | $\leq .0001$ | 1.99 |
| Posttest | 1490 | 80\% | . 15 |  |  |  |
| Honors Only |  |  |  |  |  |  |
| Pretest | 1115 | 45\% | . 26 | 53.138 | $\leq .0001$ | 2.14 |
| Posttest | 1115 | 89\% | . 13 |  |  |  |
| Males Only |  |  |  |  |  |  |
| Pretest | 1160 | 42\% | . 25 | 52.719 | $\leq .0001$ | 2.09 |
| Posttest | 1160 | 84\% | . 15 |  |  |  |
| Females Only |  |  |  |  |  |  |
| Pretest | 1445 | 43\% | . 24 | 60.288 | $\leq .0001$ | 2.05 |
| Posttest | 1445 | 84\% | . 15 |  |  |  |
| Free/Reduced Lunch Only |  |  |  |  |  |  |
| Pretest | 619 | 40\% | . 23 | 40.771 | $\leq .0001$ | 2.16 |
| Posttest | 619 | 82\% | . 15 |  |  |  |
| No Free/Reduced Lunch Only |  |  |  |  |  |  |
| Pretest | 1986 | 43\% | . 25 | 69.998 | $\leq .0001$ | 2.07 |
| Posttest | 1986 | 85\% | . 14 |  |  |  |
| Non-Minority Only |  |  |  |  |  |  |
| Pretest | 1498 | 42\% | . 24 | 62.173 | $\leq .0001$ | 2.10 |
| Posttest | 1498 | 84\% | . 15 |  |  |  |
| Minority Only |  |  |  |  |  |  |
| Pretest | 454 | 46\% | . 26 | 29.046 | $\leq .0001$ | 1.79 |
| Posttest | 454 | 84\% | . 15 |  |  |  |
| Multi-Ethnic |  |  |  |  |  |  |
| Pretest | 653 | 42\% | . 25 | 42.027 | $\leq .0001$ | 2.12 |
| Posttest | 653 | 85\% | . 14 |  |  |  |

Figures 16, 17, and 18 provide a visual look at the increases. In general, the percentage increases were about $40 \%$ for each comparison group.

Figure 16: Algebra II Module 6
Pretest and Posttest Percent Correct Scores
All Students, Basic/Honors Comparison


Figure 17: Algebra II Module 6
Pretest and Posttest Percent Correct Scores
Males/Females \& Free/Reduced Lunch/No Free Reduced Lunch


Figure 18: Algebra II Module 6
Pretest and Posttest Percent Correct Scores
Non-Minority, Minority, \& Multi-Ethnic


## Module 7

This module covers adding, subtracting, multiplying, and dividing rational expressions as well as solving rational equations. Table 12 shows that the increases from pretesting to posttesting were all statistically significant ( $\leq .0001$ ) and the effect sizes were all large. As expected, the honors students scored higher than the basic students. Other than that difference, it appears there was little difference between the various demographic groups.

Table 12: Comparison of Pretest to Posttest Percent Correct Scores
Algebra II Instructional Module 7

| Group | Number of Students | Mean | Standard Deviation | t-Test | Significance | Effect Size |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| All Students |  |  |  |  |  |  |
| Pretest | 2083 | 41\% | . 28 | 67.081 | $\leq .0001$ | 1.81 |
| Posttest | 2083 | 83\% | . 17 |  |  |  |
| Basic Only |  |  |  |  |  |  |
| Pretest | 1171 | 38\% | . 27 | 49.180 | $\leq .0001$ | 1.76 |
| Posttest | 1171 | 79\% | . 19 |  |  |  |
| Honors Only |  |  |  |  |  |  |
| Pretest | 912 | 45\% | . 29 | 45.685 | $\leq .0001$ | 1.98 |
| Posttest | 912 | 89\% | . 12 |  |  |  |
| Males Only |  |  |  |  |  |  |
| Pretest | 921 | 40\% | . 29 | 45.146 | $\leq .0001$ | 1.92 |
| Posttest | 921 | 85\% | . 16 |  |  |  |
| Females Only |  |  |  |  |  |  |
| Pretest | 1162 | 41\% | . 27 | 49.743 | $\leq .0001$ | 1.83 |
| Posttest | 1162 | 83\% | . 18 |  |  |  |
| Free/Reduced Lunch Only |  |  |  |  |  |  |
| Pretest | 485 | 39\% | . 27 | 32.998 | $\leq .0001$ | 1.86 |
| Posttest | 485 | 81\% | . 17 |  |  |  |
| No Free/Reduced Lunch Only |  |  |  |  |  |  |
| Pretest | 1598 | 41\% | . 29 | 58.415 | $\leq .0001$ | 1.81 |
| Posttest | 1598 | 84\% | . 17 |  |  |  |
| Non-Minority Only |  |  |  |  |  |  |
| Pretest | 1200 | 39\% | . 27 | 52.931 | $\leq .0001$ | 1.87 |
| Posttest | 1200 | 82\% | . 18 |  |  |  |
| Minority Only |  |  |  |  |  |  |
| Pretest | 364 | 45\% | . 30 | 24.865 | $\leq .0001$ | 1.62 |
| Posttest | 364 | 84\% | . 16 |  |  |  |
| Multi-Ethnic |  |  |  |  |  |  |
| Pretest | 519 | 43\% | . 30 | 33.424 | $\leq .0001$ | 1.89 |
| Posttest | 519 | 86\% | . 14 |  |  |  |

Figures 19, 20, and 21 provide a visual look at the increases. In general, the percentage increases were about $40 \%$ for each comparison group.

Figure 19: Algebra II Module 7 Pretest and Posttest Percent Correct Scores

All Students, Basic/Honors Comparison


Figure 20: Algebra II Module 7
Pretest and Posttest Percent Correct Scores
Males/Females \& Free/Reduced Lunch/No Free Reduced Lunch


Figure 21: Algebra II Module 7
Pretest and Posttest Percent Correct Scores
Non-Minority, Minority, \& Multi-Ethnic


## Module 8

This module covers solving and graphing exponential and logarithmic equations. Table 13 shows that the increases from pretesting to posttesting were all statistically significant ( $\leq .0001$ ) and the effect sizes were all large. As expected, the honors students scored higher than the basic students. Other than that difference, it appears there was little difference between the various demographic groups.

Table 13: Comparison of Pretest to Posttest Percent Correct Scores
Algebra II Instructional Module 8

| Group | Number of Students | Mean | Standard Deviation | t-Test | Significance | Effect Size |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| All Students |  |  |  |  |  |  |
| Pretest | 1687 | 40\% | . 25 | 56.457 | $\leq .0001$ | 1.78 |
| Posttest | 1687 | 78\% | . 17 |  |  |  |
| Basic Only |  |  |  |  |  |  |
| Pretest | 924 | 38\% | . 25 | 38.810 | $\leq .0001$ | 1.65 |
| Posttest | 924 | 74\% | . 18 |  |  |  |
| Honors Only |  |  |  |  |  |  |
| Pretest | 763 | 43\% | . 25 | 41.692 | $\leq .0001$ | 1.94 |
| Posttest | 763 | 83\% | . 15 |  |  |  |
| Males Only |  |  |  |  |  |  |
| Pretest | 736 | 40\% | . 26 | 37.641 | $\leq .0001$ | 1.82 |
| Posttest | 736 | 80\% | . 17 |  |  |  |
| Females Only |  |  |  |  |  |  |
| Pretest | 951 | 40\% | . 24 | 42.293 | $\leq .0001$ | 1.70 |
| Posttest | 951 | 76\% | . 18 |  |  |  |
| Free/Reduced Lunch Only |  |  |  |  |  |  |
| Pretest | 387 | 41\% | . 24 | 24.637 | $\leq .0001$ | 1.64 |
| Posttest | 387 | 76\% | . 17 |  |  |  |
| No Free/Reduced Lunch Only |  |  |  |  |  |  |
| Pretest | 1300 | 40\% | . 25 | 51.002 | $\leq .0001$ | 1.82 |
| Posttest | 1300 | 79\% | . 17 |  |  |  |
| Non-Minority Only |  |  |  |  |  |  |
| Pretest | 982 | 39\% | . 25 | 44.233 | $\leq .0001$ | 1.78 |
| Posttest | 982 | 77\% | . 17 |  |  |  |
| Minority Only |  |  |  |  |  |  |
| Pretest | 298 | 43\% | . 25 | 21.066 | $\leq .0001$ | 1.56 |
| Posttest | 298 | 77\% | . 18 |  |  |  |
| Multi-Ethnic |  |  |  |  |  |  |
| Pretest | 407 | 40\% | . 26 | 28.491 | $\leq .0001$ | 1.85 |
| Posttest | 407 | 80\% | . 16 |  |  |  |

Figures 22, 23, and 24 provide a visual look at the increases. In general, the percentage increases were about $40 \%$ for each comparison group.

Figure 22: Algebra II Module 8
Pretest and Posttest Percent Correct Scores
All Students, Basic/Honors Comparison


Figure 23: Algebra II Module 8 Pretest and Posttest Percent Correct Scores
Males/Females \& Free/Reduced Lunch/No Free Reduced Lunch


Figure 24: Algebra II Module 8
Pretest and Posttest Percent Correct Scores
Non-Minority, Minority, \& Multi-Ethnic


## Module 9

This module covers arithmetic and geometric sequences and series finding both recursive formulas and sums. Table 14 shows that the increases from pretesting to posttesting were all statistically significant ( $\leq .0001$ ) and the effect sizes were all large. As expected, the honors students scored higher than the basic students. Other than that difference, it appears there was little difference between the various demographic groups.

Table 14: Comparison of Pretest to Posttest Percent Correct Scores
Algebra II Instructional Module 9

| Group | Number of Students | Mean | Standard Deviation | t-Test | Significance | Effect Size |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| All Students |  |  |  |  |  |  |
| Pretest | 1400 | 42\% | . 29 | 56.636 | $\leq .0001$ | 2.02 |
| Posttest | 1400 | 88\% | . 14 |  |  |  |
| Basic Only |  |  |  |  |  |  |
| Pretest | 772 | 41\% | . 29 | 40.434 | <. 0001 | 1.95 |
| Posttest | 772 | 86\% | . 15 |  |  |  |
| Honors Only |  |  |  |  |  |  |
| Pretest | 628 | 43\% | . 30 | 39.878 | $\leq .0001$ | 2.17 |
| Posttest | 628 | 92\% | . 11 |  |  |  |
| Males Only |  |  |  |  |  |  |
| Pretest | 608 | 39\% | . 29 | 40.302 | $\leq .0001$ | 2.20 |
| Posttest | 608 | 89\% | . 14 |  |  |  |
| Females Only |  |  |  |  |  |  |
| Pretest | 792 | 44\% | . 29 | 40.364 | $\leq .0001$ | 1.93 |
| Posttest | 792 | 88\% | . 14 |  |  |  |
| Free/Reduced Lunch Only |  |  |  |  |  |  |
| Pretest | 321 | 43\% | . 28 | 24.938 | $\leq .0001$ | 1.91 |
| Posttest | 321 | 86\% | . 15 |  |  |  |
| No Free/Reduced Lunch Only |  |  |  |  |  |  |
| Pretest | 1079 | 42\% | . 30 | 51.008 | $\leq .0001$ | 2.03 |
| Posttest | 1079 | 89\% | . 13 |  |  |  |
| Non-Minority Only |  |  |  |  |  |  |
| Pretest | 820 | 41\% | . 28 | 44.996 | $\leq .0001$ | 2.12 |
| Posttest | 820 | 88\% | . 14 |  |  |  |
| Minority Only |  |  |  |  |  |  |
| Pretest | 245 | 47\% | . 31 | 20.050 | $\leq .0001$ | 1.70 |
| Posttest | 245 | 88\% | . 14 |  |  |  |
| Multi-Ethnic |  |  |  |  |  |  |
| Pretest | 335 | 40\% | . 30 | 28.782 | $\leq .0001$ | 2.12 |
| Posttest | 335 | 89\% | . 13 |  |  |  |

Figures 25,26 , and 27 provide a visual look at the increases. In general, the percentage increases were about $40 \%$ to $45 \%$ for each comparison group.

Figure 25: Algebra II Module 9
Pretest and Posttest Percent Correct Scores
All Students, Basic/Honors Comparison


Figure 26: Algebra II Module 9
Pretest and Posttest Percent Correct Scores
Males/Females \& Free/Reduced Lunch/No Free Reduced Lunch

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Figure 27: Algebra II Module 9
Pretest and Posttest Percent Correct Scores
Non-Minority, Minority, \& Multi-Ethnic


## Conclusions

The conclusions will review the data analyzed to answer each of the three questions that guided this study.

Question 1: Do students enrolled in the Florida Virtual School Algebra II program increase their knowledge and skills in Algebra II?

For each of the comparisons across the 9 modules, the increases were statistically significant ( $\leq .0001$ ), indicating a difference that would occur by chance less than 1 out of 10,000 repetitions. The effect size, an even more significant estimate of the strength of a change, was very large for all of the modules. Perhaps of even greater significance is that the growth from pretesting to posttesting increased across the 9 modules.

The average percent increase for all students across the 9 modules is shown in Table 15.
Table 15: Gain Scores Across 9 Modules for All students

| Pretest Percent | Posttest Percent | Gain |
| :---: | :---: | :---: |
| $46 \%$ | $82 \%$ | $36 \%$ |

The conclusion to question 1 is that the module pretest/posttest comparison show significant increases for each of the modules and thus for the total Algebra II course.

Question 2: Do students enrolled in basic or honors courses achieve similar gains in the Florida Virtual School Algebra II program?

Overall, the honors students scored higher than the basic students on the pretests for all modules. The basic and honors students' average percent increases across the 9 modules are shown in Table 16.

Table 16: Gain Scores Across 9 Modules for All students

| Group | Pretest Percent | Posttest Percent | Gain |
| :---: | :---: | :---: | :---: |
| Basic | $43 \%$ | $78 \%$ | $35 \%$ |
| Honors | $50 \%$ | $87 \%$ | $37 \%$ |

Although honors students had higher average pretest and average posttest scores than basic students, both groups achieved similar average percentage gains across the 9 modules.

Question 3: Do students with differing demographic characteristics (gender, socio-economic, and ethnicity status) achieve similar gains when enrolled in the Florida Virtual School Algebra II program?

The average percent increase for male and female; higher socio-economic level and lower socio-economic level; and white, minority, and multi-ethnic students across the 9 modules are shown in Table 17.

Table 17: Gain Scores Across 9 Modules for All students

| Group | Pretest Percent | Posttest Percent | Gain |  |
| :---: | :---: | :---: | :---: | :---: |
| Gender Groups |  |  |  |  |
| Female | $46 \%$ | $81 \%$ | $35 \%$ |  |
| Male | $46 \%$ | $83 \%$ | $37 \%$ |  |
| Socio-Economic Groups |  |  |  |  |
| Lower | $46 \%$ | $80 \%$ | $34 \%$ |  |
| Higher | $46 \%$ | $83 \%$ | $37 \%$ |  |
| Ethnic Groups |  |  |  |  |
| White | $45 \%$ | $82 \%$ | $37 \%$ |  |
| Minority | $49 \%$ | $81 \%$ | $32 \%$ |  |
| Multi-Ethnic | $47 \%$ | $83 \%$ | $36 \%$ |  |

The conclusion to question 3 is that there seem to be very minor and non-consistent differences for gender, socio-economic status, and ethnicity. Students overall, regardless of demographic differences, made statistically significant and large effect size gains from pretesting to posttesting.

> The overall conclusion based on the gain scores across the 9 module pretests and posttests is that all students made statistically significant and large effect size gains from pretesting to posttesting. Honors students scored higher than basic students, but the gains made by each group were similar. The demographic comparisons showed that the program is equally effective regardless of gender, socio-economic status, and ethnicity.

